DIATHEMATIKON PROGRAMMA CROSS-THEMATIC CURRICULUM FRAMEWORK FOR MATHEMATICS

1. Teaching/learning aim

The aim of teaching Mathematics, which can be placed among the general aims of school education, is to facilitate the pupils' personal development and provide them with the necessary skills for their smooth social integration.

Mathematics can help pupils develop structured and critical thinking abilities and improve their reasoning abilities of analysis, abstraction and generalisation that will enable them to express their thoughts in a neat, clear, simple and accurate way.

Mathematics also sharpens pupils' abilities of observation, self-concentration and persistence, stimulate their initiative, creative imagination and freethinking and develop their sense of order, harmony and beauty.

Mathematics is a necessary tool in everyday life, especially at the workplace, and has a significant contribution to the development of other scientific fields, especially Technology, Economics and Social Studies.

2. Content Guiding Principles, Goals, Indicative Fundamental Cross-thematic Concepts

I. Primary school

| Grade | Content Guiding Principles | General Goals (Knowledge, skills, attitudes and values) | Indicative Fundamental Cross-thematic Concepts |
|-----------------|----------------------------|---|--|
| | | Pupils should: | |
| 1 st | Problem solving | explore mathematical situations; | Change |
| 2 nd | | | Interaction |
| 3 rd | | make enquiries; | System |
| 4 th | | | Communication |
| | | pose problems and formulate questions | Individual- |
| 5 th | | from everyday life and mathematical | Group/ Ele- |

| 6 th | | situations, rephrase problems, recognize and describe similar problems and mathematical situations, investigate open- ended problems; | ment-Set Similarity- Difference |
|-----------------|-------------|--|---------------------------------|
| | | use calculators, computers and other resources; | |
| | | apply their mathematical skills in every | |
| 1 st | Numbers and | day life situations. count orally, read, order and write natural | Change |
| 1 | operations | numbers up to 100; | Communication |
| | operations | numbers up to 100, | Individual- |
| | | add or subtract natural numbers no greater | Group/ Ele- |
| | | than 20; | ment-Set |
| | | | Similarity- |
| | | become familiar with situations that entail | Difference |
| | | multiplication and division, such as equal | |
| | | groupings of objects and sharing equally. | |
| | Measurement | become familiar with the concepts of | Change |
| | | length, time, money and mass; | System |
| | | | Space-Time |
| | | describe, extend and make generalizations | Similarity- |
| | | about geometric and numeric patterns. | Difference |
| | Geometry | develop spatial sense, draw, reproduce, | System Communication |
| | | recognize, name and classify geometrical figures; | Space-Time |
| | | figures, | Similarity- |
| | | identify solids: cubes, rectangular prisms, cylinders, spheres; | Difference |
| | | recognize reflective symmetry in pictures and figures. | |

| 2 nd | Numbers and | count orally, read, write and order natural | Change |
|-----------------|-------------|---|-------------|
| | operations | numbers up to 1,000; | System |
| | | | Space-Time |
| | | add, subtract and multiply numbers no | Individual- |
| | | greater than 100; | Group/ Ele- |
| | | | ment-Set |
| | | use the commutative and associative | Similarity- |
| | | property in addition and multiplication; | Difference |
| | | | |
| | | understand division as a process of equal | |
| | | sharing. | |
| | Measurement | measure length and surface using standard | Change |
| | | and non-standard units; | System |
| | | | Space-Time |
| | | measure time, money and mass; | Individual- |
| | | | Group/ Ele- |
| | | describe, extend and make generalizations | ment-Set |
| | | about geometric and numeric patterns. | Similarity- |
| | | acout geometre une nomerre puntans. | Difference |
| | Geometry | draw and reproduce geometrical figures | Change |
| | | and recognize their geometrical features; | Interaction |
| | | | System |
| | | define points and draw segments and | Culture |
| | | straight lines; | Individual- |
| | | | Group/ Ele- |
| | | recognize by experience parallel and ver- | ment-Set |
| | | tical lines; | Similarity- |
| | | | Difference |
| | | identify solids (cubes, rectangular prisms, | |
| | | cylinders, spheres); | |
| | | | |
| | | recognize reflective symmetry of a | |
| | | geometrical figure and use rules of | |
| | | symmetry to complete a figure design. | |

| 3 rd | Numbers and | count orally, read, write and order, natural | Change |
|-----------------|-------------|--|-------------------------|
| | operations | numbers up to 10,000; | Interaction |
| | | | System |
| | | add, subtract and multiply natural num- | Individual- |
| | | bers no greater than 1,000; | Group/ Ele- |
| | | | ment-Set |
| | | develop number sense for fractions and | Similarity- |
| | | decimals; | Difference |
| | | | |
| | | become familiar with the algorithm of | |
| | | multiplication and division of natural | |
| | | numbers. | |
| | Measurement | identify and use the measurement units of | Change |
| | | length, time and mass; | Interaction |
| | | | System |
| | | recognize a pattern and understand that | Space-Time |
| | | iteration processes are infinite. | |
| | Geometry | describe, reproduce and draw figures and | System |
| | | solids by means of vertical lines drawn | Space-Time |
| | | with the help of instruments; | Symmetry |
| | | | Individual- |
| | | become familiar with vertices, edges, | Group/ Ele- |
| | | right angles and sides; | ment-Set Similarity- |
| | | draw symmetrical figures using reflective | Difference |
| | | symmetry. | |
| 4 th | Numbers and | count orally, read, write and order natural | Change |
| | operations | numbers up to 1,000,000; | System |
| | | | Individual- |
| | | add, subtract and multiply natural num- | Group |
| | | bers no greater than 1,000; | Similarity- |
| | | | Difference |
| | | perform operations with decimal numbers | |
| | | and decimal fractions. | |

| | Measurement | measure length, area, time, mass and ca- | Change |
|-----------------|-----------------|--|--------------|
| | | pacity; | System |
| | | | Space-Time |
| | | convert units of measurement and practise | Culture |
| | | additions and subtractions using com- | Individual- |
| | | pound numbers; | Group/ Ele- |
| | | | ment-Set |
| | | become familiar with simple numerical | Similarity- |
| | | and geometrical patterns. | Difference |
| | Geometry | draw parallel and vertical lines as well as | System |
| | | geometrical shapes with the use of appro- | Space-Time |
| | | priate instruments; | Individual- |
| | | | Group/ Ele- |
| | | calculate the perimeter of simple figures | ment-Set |
| | | | Symmetry |
| | | understand intuitively the concept of sur- | Similarity- |
| | | face; | Difference |
| | | | |
| | | construct reflective figures on squared | |
| | | paper. | |
| | Gathering and | practice collecting, classifying, represent- | System |
| | processing data | ing and interpreting data; | Organization |
| | | | |
| | | develop an appreciation for the use of | |
| | | probability in the real world. | |
| 5 th | Numbers and | count orally, read write and order natural | System |
| | operations | numbers up to 100,000,000 as well as | Individual- |
| | | fractions and decimals; | Group/ Ele- |
| | | | ment-Set |
| | | add, subtract, multiply and divide natural | Similarity- |
| | | numbers, fractions and decimals; | Difference |
| | | add and subtract compound numbers | |
| | | | |
| | | | |

| | find the multiples of 2, 3,, 10; | |
|-----------------|---|----------------|
| | 1 , , , , , | |
| | know which numbers are divided by 2, 5 | |
| | and 10. | |
| Measurement | consolidate knowledge of standard meas- | Change |
| Wieasurement | | O |
| | urement units of length, area, mass, time | System |
| | and capacity and be able to apply these | Space-Time |
| | measurements in every day life; | Culture |
| | | Similarity- |
| | recognize, describe and extend simple | Difference |
| | arithmetic and geometrical patterns. | |
| Geometry | draw geometrical figures with the help of | Change |
| | instruments; | System |
| | | Space-Time |
| | calculate perimeter and area of basic | Individual- |
| | geometrical figures and circumference of | Group/ Ele- |
| | circles; | ment-Set |
| | | Similarity- |
| | name, classify and draw angles and trian- | Difference |
| | gles; | Classification |
| | | |
| | draw expansions of simple solids. | |
| Gathering and | develop an understanding of the concept | Change |
| processing data | of ordered pair; | System |
| processing data | or ordered pair, | Space-Time |
| | be able to read, interpret and create | Individual- |
| | | |
| | graphs, bar charts, pictographs and tabu- | Group/ Ele- |
| | late data; | ment-Set |
| | | Similarity- |
| | become familiar with the concept of prob- | Difference |
| | ability, make predictions and calculate | Probability |
| | mean. | |
| | | |
| • | • | |

| 6 th | Numbers and | count orally, read, write and order natural | System |
|-----------------|-----------------|--|-------------|
| | operations | numbers, fractions and decimals and use | Individual- |
| | | them in numerical operations; | Group/ Ele- |
| | | | ment-Set |
| | | learn which numbers are divided by 2, 3, | Similarity- |
| | | 4, 5, 9, 10 and 25; | Difference |
| | | | Analysis- |
| | | analyse natural numbers in prime factors | synthesis |
| | | and powers. | |
| | Measurement | consolidate knowledge of standard meas- | Change |
| | | urement units of length, area, mass, time | System |
| | | and capacity and be able to apply these | Space-Time |
| | | measurements in every day life; | Individual- |
| | | | Group/ Ele- |
| | | state rules for simple numerical or geo- | ment-Set |
| | | metrical patterns. | Similarity- |
| | | | Difference |
| | Geometry | design rectilinear figures and circles using | Change |
| | | ruler and compass; | System |
| | | | Space-Time |
| | | calculate circumference and area of cir- | Individual- |
| | | cles as well as area and volume of solids; | Group/ Ele- |
| | | | ment-Set |
| | | draw and compare angles; | Similarity- |
| | | | Difference |
| | | draw reflective figures; | Symmetry |
| | | | |
| | | use rules of reflective symmetry; | |
| | | | |
| | | translate and scale up or down geometri- | |
| | | cal figures. | |
| | Gathering and | collect and record data; | Change |
| | processing data | | System |

| Statistics | create data tables and graphs (bar charts, | Communication |
|-----------------|---|---------------|
| | histograms); | Space-Time |
| | | Individual- |
| | report data on graphs orally or in the form | Group/ Ele- |
| | of written paragraph; | ment-Set |
| | | Similarity- |
| | transfer data from text to table or graph | Difference |
| | | |
| | make predictions; | |
| | | |
| | understand the concept of the ordered pair | |
| | and calculate mean. | |
| Ratios and pro- | use proportional reasoning to solve prob- | System |
| portions | lems ("Simple Method of Three"); | Individual- |
| | | Group/ Ele- |
| | understand and apply ratios, proportions | ment-Set |
| | and percentages. | Similarity- |
| | | Difference |
| Equations | solve simple equations based on operation | System |
| | definitions. | Individual- |
| | | Group/ Ele- |
| | | ment-Set |
| | | Similarity- |
| | | Difference |

II. Junior High school

| | | | Indicative |
|-----------------|------------------------|---|----------------|
| | Content Guiding | Goals | Fundamental |
| Grade | Principles | (Knowledge, skills, attitudes, and | Cross-thematic |
| | | values) | Concepts |
| | | Pupils should: | |
| 1 st | Arithmetic- | develop fluency in operations of | Group/Set |
| | Algebra | natural numbers, fractions and deci- | System |
| | Arithmetic and | mals and use their properties to solve | Change |
| | algebraic calculus | equations and problems; | Communication |
| | | | Equality |
| | | develop an understanding of negative | Equivalence |
| | | rational numbers and be able to solve | |
| | | equations and problems involving | |
| | | rational numbers in general. | |
| | Proportions | apply ratios as well as direct and in- | Similarity |
| | Direct and Inverse | verse proportion to solve problems | Change |
| | proportion | from everyday life situations (e.g. | System |
| | | percentages, distribution, etc). | Interaction |
| | | | |
| | Geometry | become familiar with basic geometri- | Space-Time |
| | Geometrical con- | cal concepts like point, segment, | Group/Set |
| | cepts | straight line, angle, rectilinear figure, | System |
| | Geometrical fig- | circle, arc (of a circle), central angle, | Change |
| | ures | etc and understand their importance | Communication |
| | | in Geometry; | Culture |
| | | | Art |
| | | understand perpendicularity, parallel- | Similarity- |
| | | ism and reflective or rotational sym- | Difference |
| | | metry and use them to analyse | |
| | | mathematical situations (e.g. proper- | |
| | | ties of triangles, parallelograms, etc). | |

| | Measurement | understand the concepts of length of | Change |
|-----------------|------------------|---|---------------|
| | | segment and measure of angle and | Interaction |
| | | arc, using appropriate units of | Space-Time |
| | | measurement. | Similarity- |
| | | | Difference |
| 2 nd | Algebra- | understand operations and properties | Group/Set |
| | Statistics | of irrational and real numbers and be | Communication |
| | Algebraic Calcu- | able to use them to solve problems | Change |
| | lus | involving linear equations and ine- | Similarity- |
| | | qualities. | Difference |
| | Functions | develop an initial conceptual under- | Interaction |
| | | standing of functions; | Communication |
| | | | Change |
| | | interpret and translate among tabular, | Similarity- |
| | | symbolic and graphical representa- | Difference |
| | | tions of functions; | Culture |
| | | | |
| | | use different representations of func- | |
| | | tions $y = ax$ and $y = \frac{a}{x}$ to solve | |
| | | problems in everyday life situations | |
| | | (e.g. direct and inverse proportion, | |
| | | etc.). | |
| | Statistics | read, understand and interpret statis- | Group |
| | | tical representations (tables, graphs, | Interaction |
| | | diagrams); | Communication |
| | | | Change |
| | | collect, organize and display statisti- | System |
| | | cal data and draw conclusions. | |
| | Geometry | develop an understanding of the con- | Space-Time |
| | Geometrical con- | cept of angle inscribed in a circle and | Communication |
| | cepts | of the regular polygons and their role | Similarity- |
| | Geometrical fig- | in measuring circumference and cir- | Difference |
| | I | I | · |

| | ures | cular area; | System |
|-----------------|-------------------|---------------------------------------|---------------|
| | | | |
| | | recognize basic solids (prism, cylin- | |
| | | der, pyramid, cone and sphere) and | |
| | | understand their properties. | |
| | Measurement | understand units of measurement for | Interaction |
| | | area and volume; | Communication |
| | | | Similarity- |
| | | measure area of plane figures and | Difference |
| | | solids; | System |
| | | | |
| | | measure volume of solids (prism, | |
| | | cylinder, cone and sphere). | |
| | Trigonometry- | develop an understanding of trigo- | Similarity |
| | Vectors | nometric numbers of oblique angles | Change |
| | | and how they are related; | System |
| | | | Interaction |
| | | understand vectors; | |
| | | | |
| | | add and subtract vectors; | |
| | | | |
| | | analyze vectors in two perpendicular | |
| | | components. | |
| 3 rd | Algebra- | develop an uunderstanding of alge- | Communication |
| | Statistics | braic expressions and especially mo- | Similarity– |
| | Algebraic Calcu- | nomials, polynomials and rational | Difference |
| | lus | expressions and their properties and | System |
| | | be able to perform operations; | S J 500 222 |
| | | or acte to perform operations, | |
| | | understand the basic algebraic formu- | |
| | | las; | |
| | | 140, | |
| | | he able to feetowize and simulify -1 | |
| | | be able to factorize and simplify al- | |

| | gebraic expressions. | |
|--------------------|---|---------------|
| Equations – | solve, both algebraically and graphi- | Interaction |
| inequalities- | cally, simple and quadratic equations, | Similarity- |
| systems | simple inequalities and linear sys- | Difference |
| | tems. | Equality |
| | | System |
| Functions | apply different representations of | Interaction |
| | function $y = ax^2 + bx + c$ in problem | Change |
| | solving. | Similarity- |
| | 55 | Difference |
| Probability | understand and apply the basic con- | Group/Set |
| | cepts and laws of theoretical prob- | Communication |
| | ability (sample space, event, classical | System |
| | definition of probability). | Probability |
| Geometry | understand and apply congruency, | Space-Time |
| Geometrical con- | and especially equal triangles to | Communication |
| cepts | solve geometrical problems; | Similarity- |
| Geometrical fig- | | Difference |
| ures | understand ratios, Thales theorem, | Culture |
| | figure similarity and especially trian- | System |
| | gle similarity and apply them to solve | |
| | everyday life problems. | |
| Trigonometry | develop an understanding of sine, | |
| Sine, Cosine and | cosine and tangent of an angle not | |
| Tangent Ratios | greater than 360° and their relations; | |
| | | |
| | understand sine and cosine rules and | |
| | apply them to solve triangle prob- | |
| | lems. | |
| | | |